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Study of crack propagation by infrared thermography during very high cycle fatigue regime

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Introduction

- Many elements of mechanical structures can be loaded beyond 10^7 cycles :
 - ⇒ Very high cycle fatigue regime (VHCF) or gigacycle fatigue regime
- Fracture mechanisms associated with the VHCF are different from those known in high cycle fatigue (HCF) :
 - Fatigue failure can occur at values of cycle exceed 10^7 cycles and for stress level below the conventional high cycle fatigue limit.
 - In high yield strength steels the fracture does not occur on the surface but rather internally in the materials : formation of a fish eye

Experimental study of the crack propagation in the VHCF regime

- Experimental difficulties :

- High frequency : In gigacycle fatigue test is carried out at ultrasonic frequency (20kHz) one cycle : 50 μ s
- Test duration : 14 hours for 10⁹ cycles
- Internal crack initiation

⇒ Is it possible to use pyrometry to understand and to study the fatigue initiation in VHCF regime?

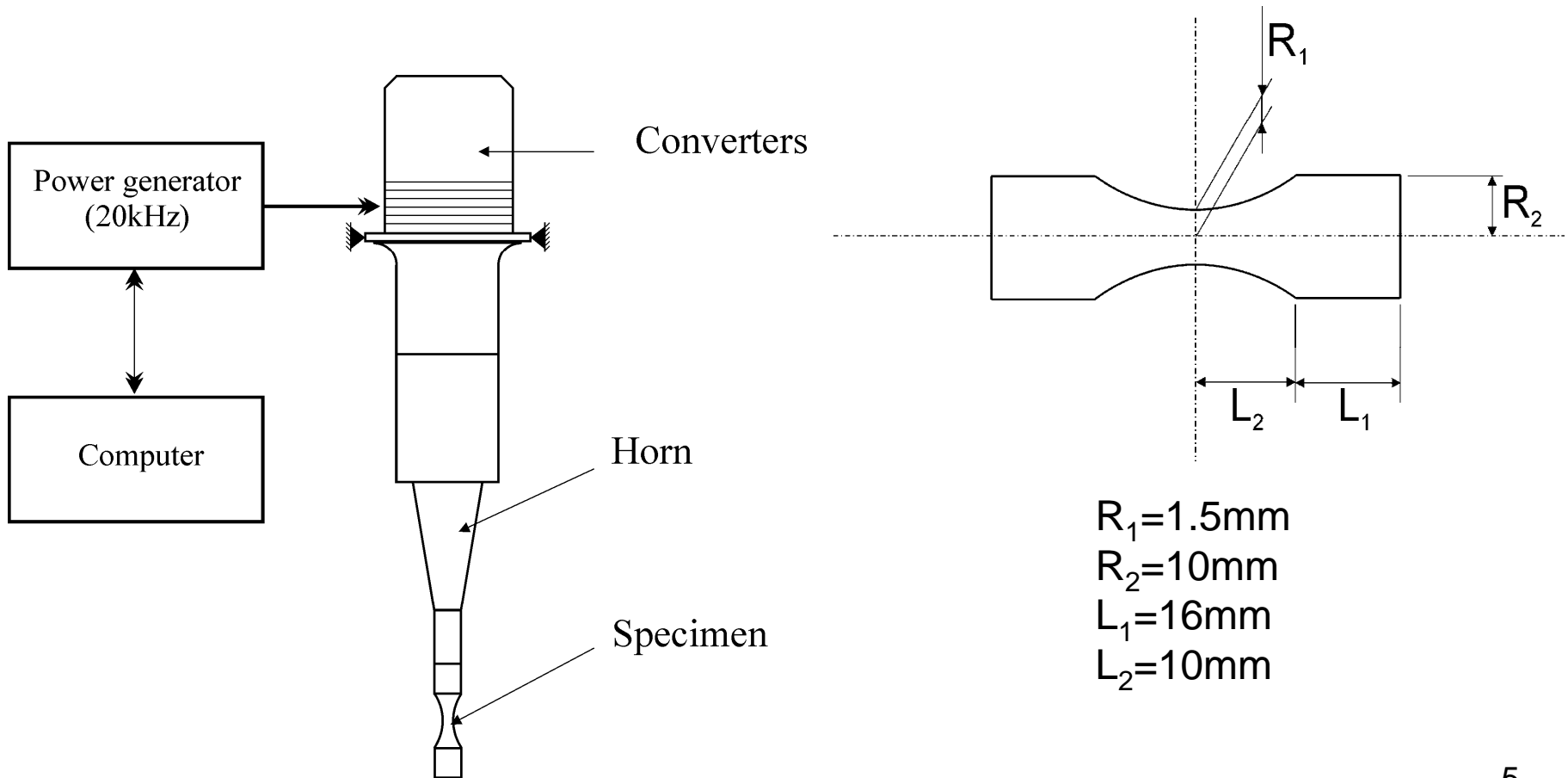
- Advantage of pyrometry technique:

- Good spatial and time resolutions
- It allows to obtain field measurements on the surface of the specimen
- The dissipated power is higher than at low frequency
- It allows to detect the thermal effects associated with an internal crack propagation (the fish eye formation, i.e. crack propagation , inside the material in the gigacycle fatigue regime is related to a local increase of the temperature due to plasticity on the crack tip.)

Experimental device : ultrasonic
fatigue test with measurement of
temperature fields

Experimental device : ultrasonic fatigue test

- Ultrasonic fatigue machine
- Geometry of the specimen



Experimental device : temperature field measurement



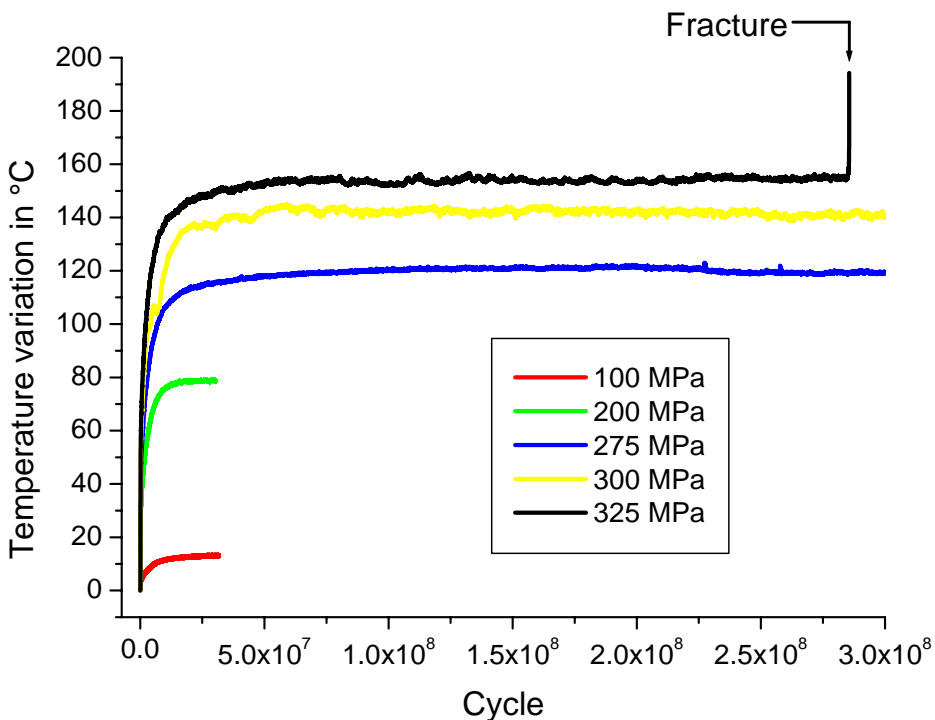
- **Temperature measurement by infrared pyrometry:**

- MCT detector
- Wavelength range : $3.7\mu\text{m} - 4.9\mu\text{m}$
- Aperture time : $100\mu\text{s} - 1500\mu\text{s}$
- Refresh time : $16\text{ms} - 40\text{ms}$
- Spatial resolution : 0.12mm/pixel

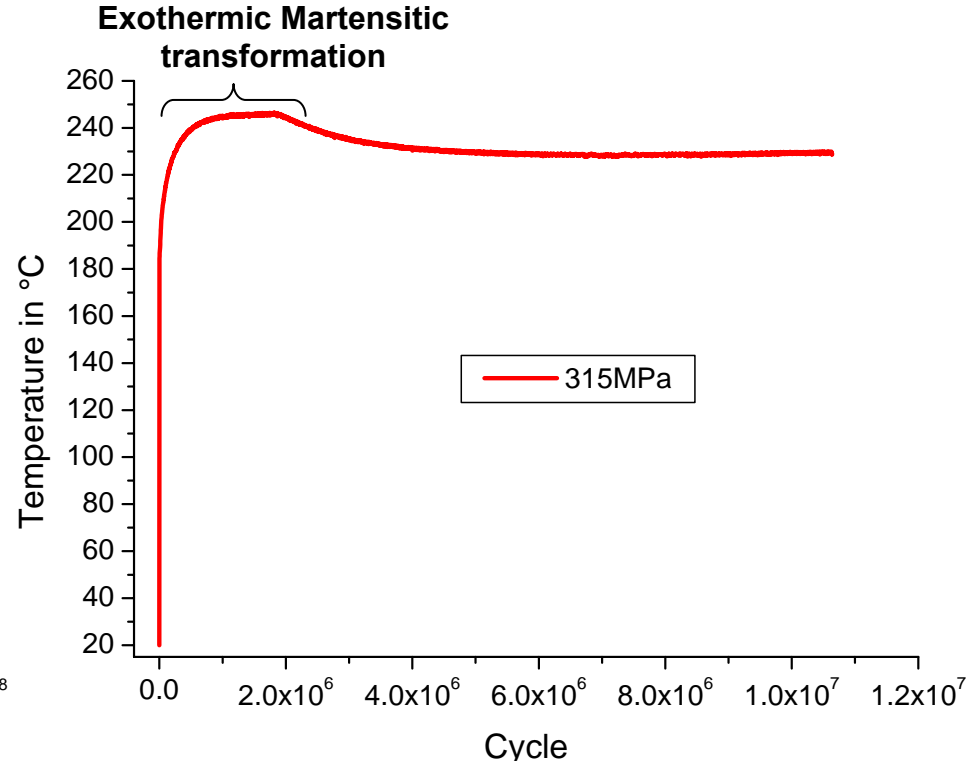
Experimental device : test with $R=0.01$

Temperature evolution during an ultrasonic fatigue test

- **Case of a high-strength steel :** (0.22% of C; 1.22% of Mn; 1% of Cr; 1% of Ni); **UTS = 950MPa**



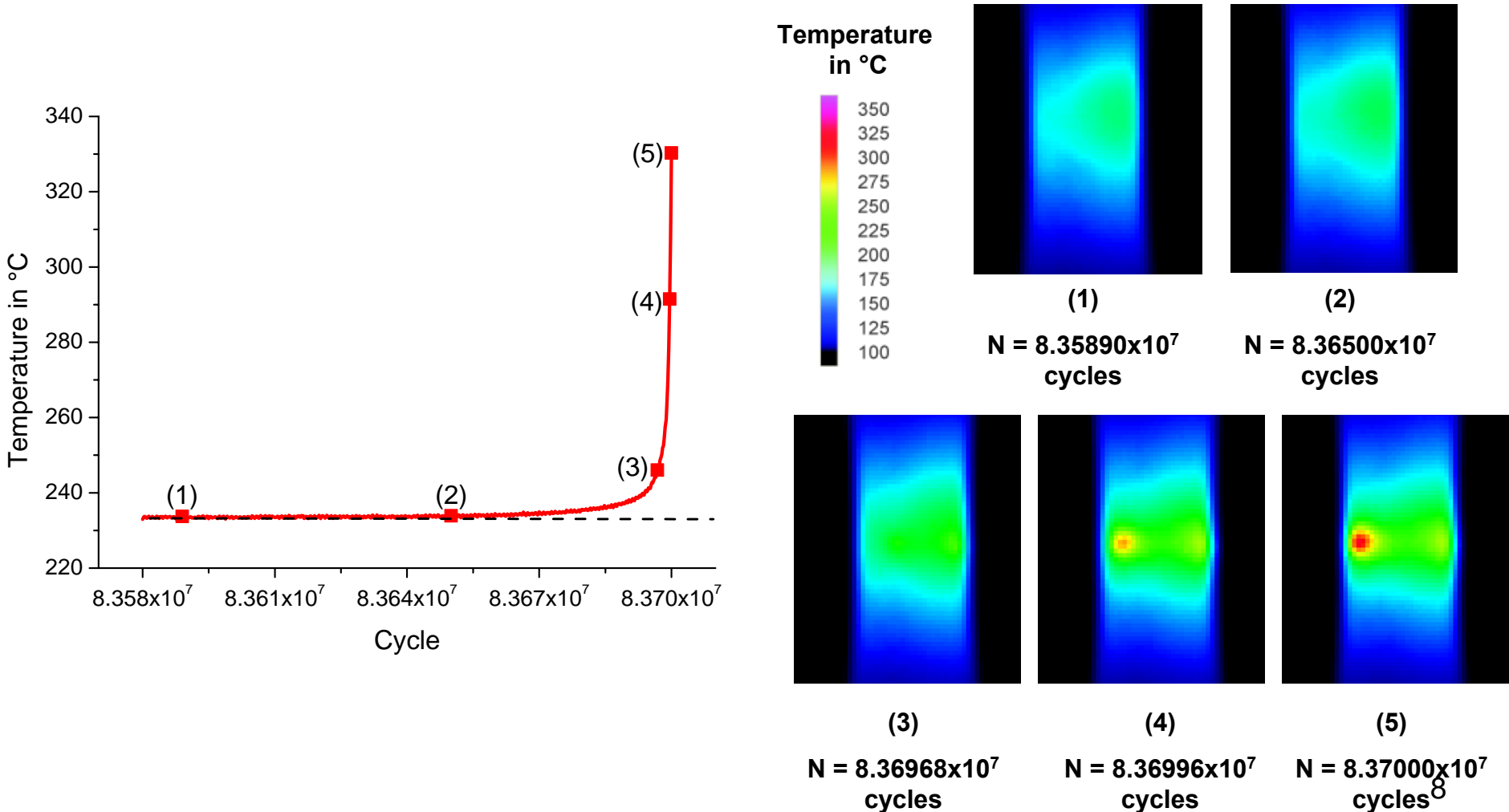
- **Case of another high-strength steel :** (0.22% of C; Mn, Cr, Si: less than 1%); **UTS ≈ 1700MPa**



Specimen is cooled by an air circulation in order to limit its heating

Temperature field just before the fracture

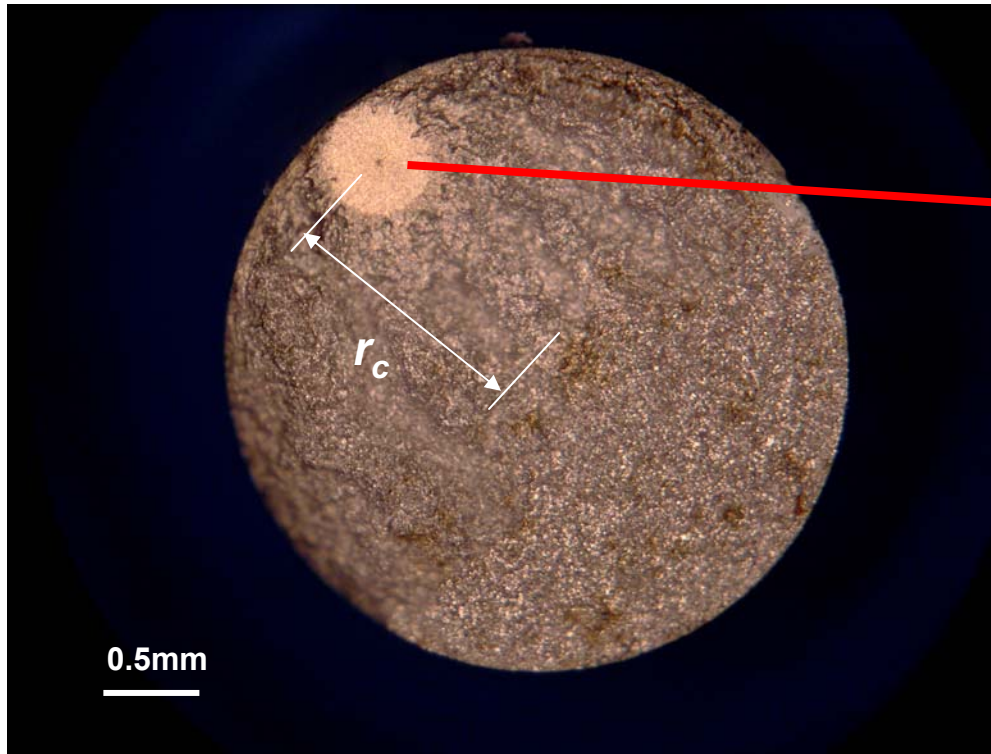
- $R=-1$; $\Delta\sigma=335\text{MPa}$; $N_F=8.37\times 10^7$ cycles (gigacycle domain)



Post mortem observation of the fracture surface

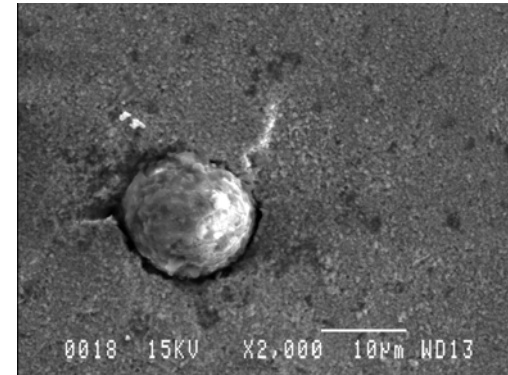
- Optical microscopy

↓ Observation direction



Propagation of a fish eye fatigue crack

- Scanning electronic microscopy



Inclusion in the center of the fatigue crack :

- ⇒ **Average radius of the inclusion: $a_{int}=7.6\mu\text{m}$**
- ⇒ **Eccentricity: $e=r_c/R_1=0.81$**

Thermal model of the crack propagation

The model of crack propagation 1

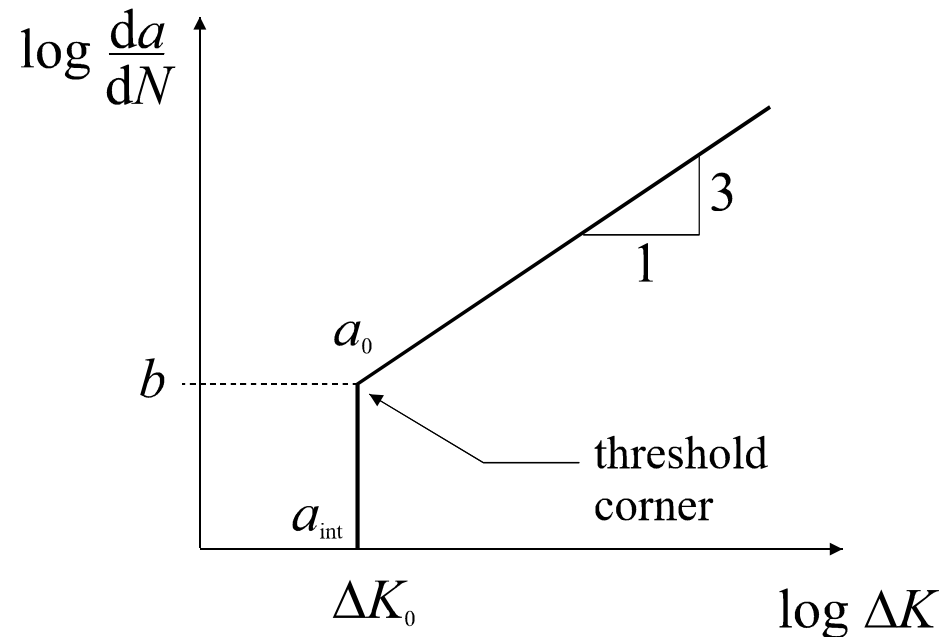
- **Paris-Hertzberg-McClintock crack growth rate law :**

$$\frac{da}{dN} = b \left(\frac{\Delta K_{eff}}{E\sqrt{b}} \right)^3$$

b norm of the Burgers vector
 E Young modulus

- **On the threshold corner**

$$\frac{da}{dN} = b \quad \text{and} \quad \frac{\Delta K_0}{E\sqrt{b}} = 1$$



The model of crack propagation 2

By supposing a circular crack and neglecting crack closure:

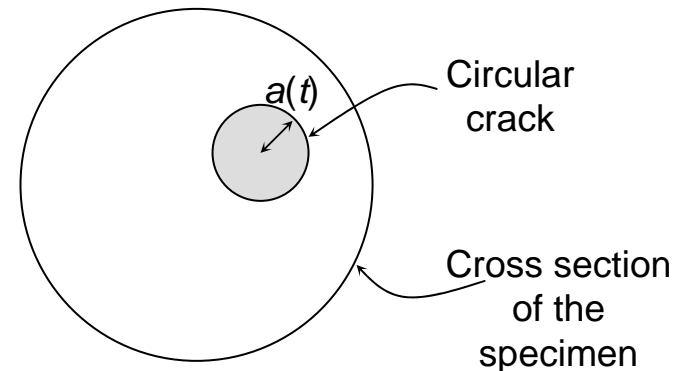
$$\Delta K_{eff} = \Delta K = \frac{2}{\pi} \Delta \sigma \sqrt{\pi a}$$

The crack growth rate law is thus written:

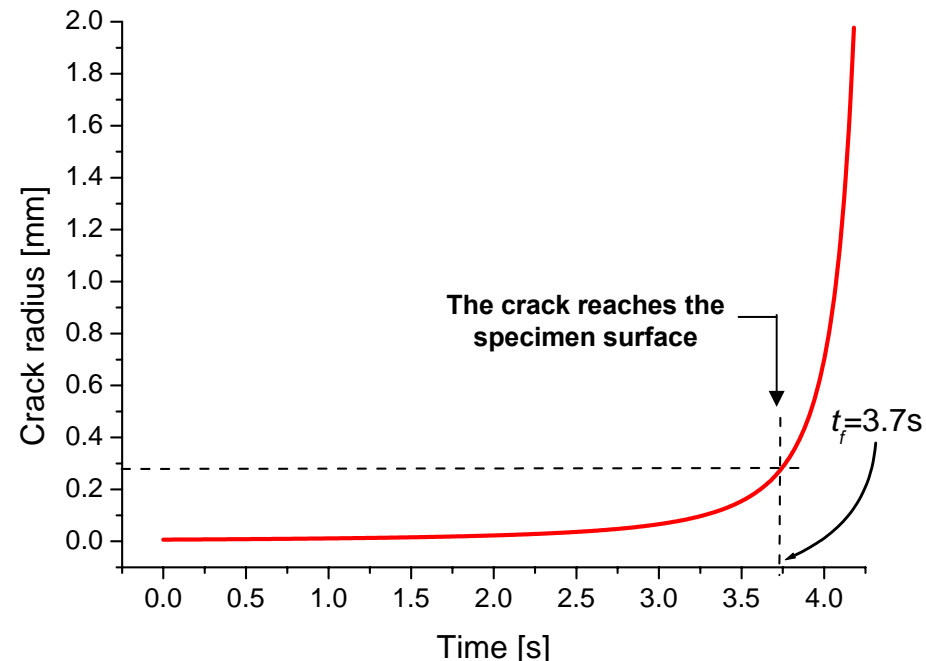
$$\frac{da}{dN} = b \left(\frac{\Delta K}{\Delta K_0} \right)^3 = b \left(\frac{a}{a_0} \right)^{3/2}$$

After integration between a_0 ($t=0$) and a (time t):

$$a(t) = \frac{a_0}{\left(1 - \frac{t}{t_c}\right)^2} \quad \text{with} \quad t_c = \frac{2a_0}{bf}$$



Geometry of the circular crack



Evolution of the crack radius¹²
($a_0=8\mu\text{m}$; $e=0.8$; $t_c=4.4s$)

Calculation of the dissipated energy during crack growth

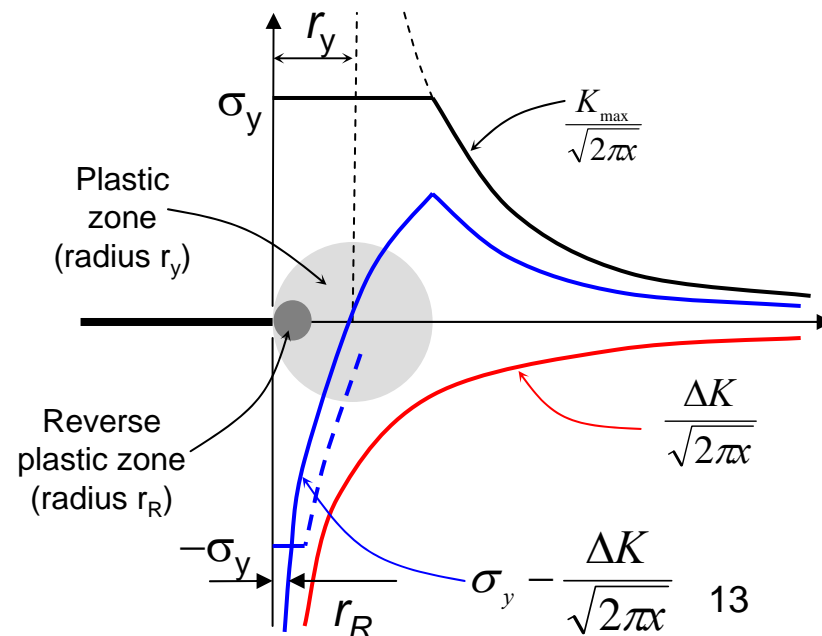
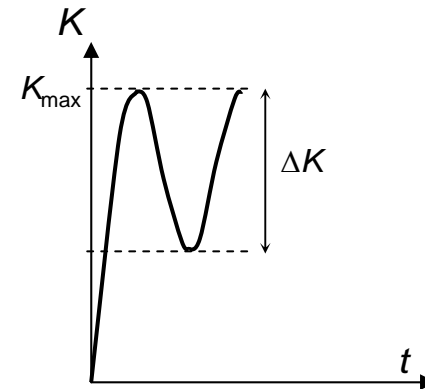
- The reverse plastic zone size in plane strain:

$$r_R = \frac{r_y}{4} = \frac{1}{6\pi} \frac{\Delta K^2}{(2\sigma_y)^2}$$

$$r_R < 0.13 \mu\text{m}$$

- Energy dissipated per unit length of crack:

$$E = \eta r_R^2$$



Calculation of the dissipated energy during crack growth

Evolution of the dissipated energy versus time:

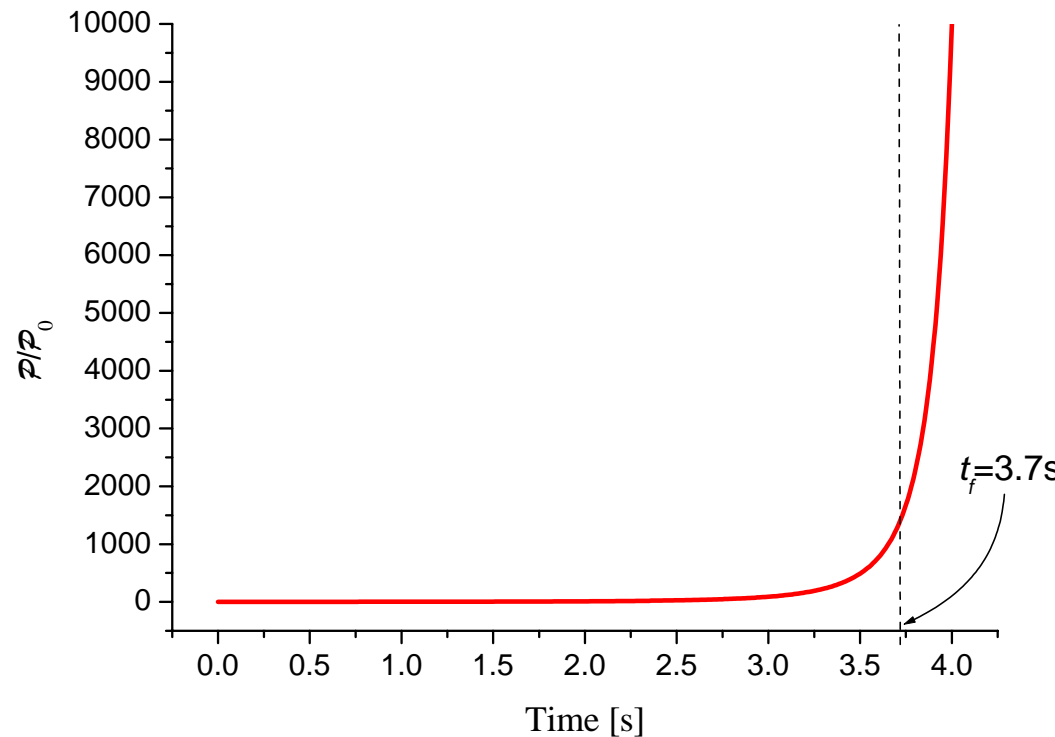
$$E = \eta r_R^2 = \eta \frac{\Delta K^4}{24^2 \pi^2 \sigma_y^4}$$

$$E = \eta \frac{a^2}{36\pi^4 \sigma_y^4} = \eta \frac{a_0^2 \Delta \sigma^4}{36\pi^4 \sigma_y^4 \left(1 - \frac{t}{t_c}\right)^4}$$

Evolution of the dissipated power versus time:

$$P = Ef = \frac{P_0}{\left(1 - \frac{t}{t_c}\right)^4} \quad \text{with} \quad t_c = \frac{2a_0}{bf}$$

P_0 is a constant which is identified from experimental data



Evolution of dissipated power
($a_0=8\mu\text{m}$; $e=0.8$; $t_c=4.4$ s)

Modeling of the thermal problem

- Thermal model assumptions:
 - The specimen is modeled by a cylinder with a radius of $R_1=1.5\text{mm}$
 - For symmetry reasons, only one half of the specimen is considered
 - r_R is very small (about $0.13\mu\text{m}$) : the fatigue crack is modeled by a dissipated power along the crack tip (P is the dissipated power per unit length)

Heat transfer equation

- Heat transfer equation:

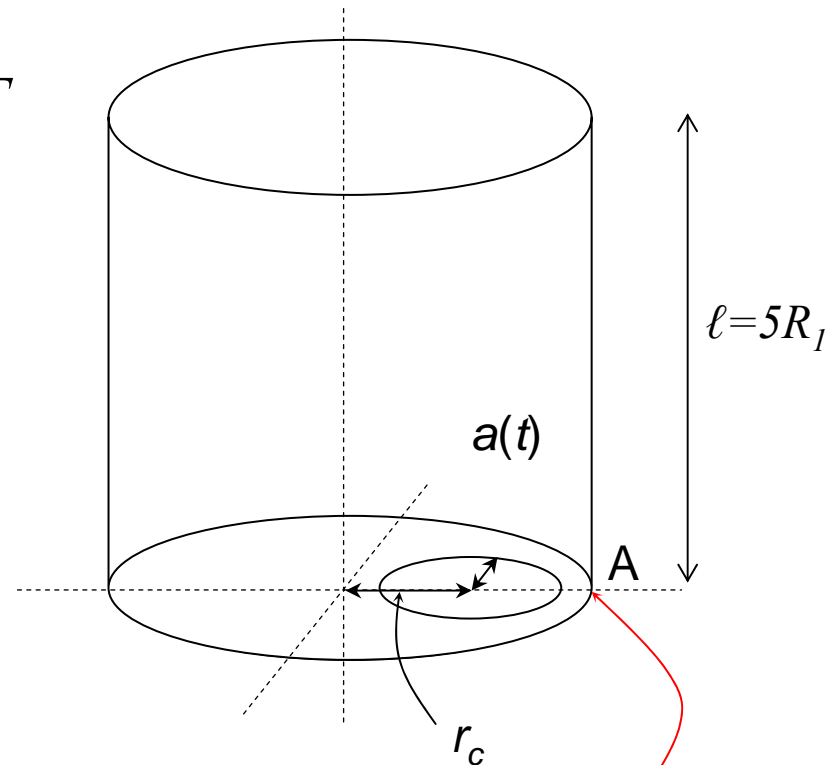
$$\rho C \frac{\partial T}{\partial t} = \frac{P(t)}{2} \delta(r_c - a(t)) \delta(z) + \lambda \Delta T$$

- Initial condition

$$T(t = 0) = T_0$$

- Boundary condition
(adiabatic conditions)

$$\frac{\partial T}{\partial r}(r = R_1) = 0 \quad \frac{\partial T}{\partial z}(z = \ell) = 0 \quad \frac{\partial T}{\partial z}(z = 0) = 0$$



Maximum surface temperature 16

Numerical simulation of the temperature field 1

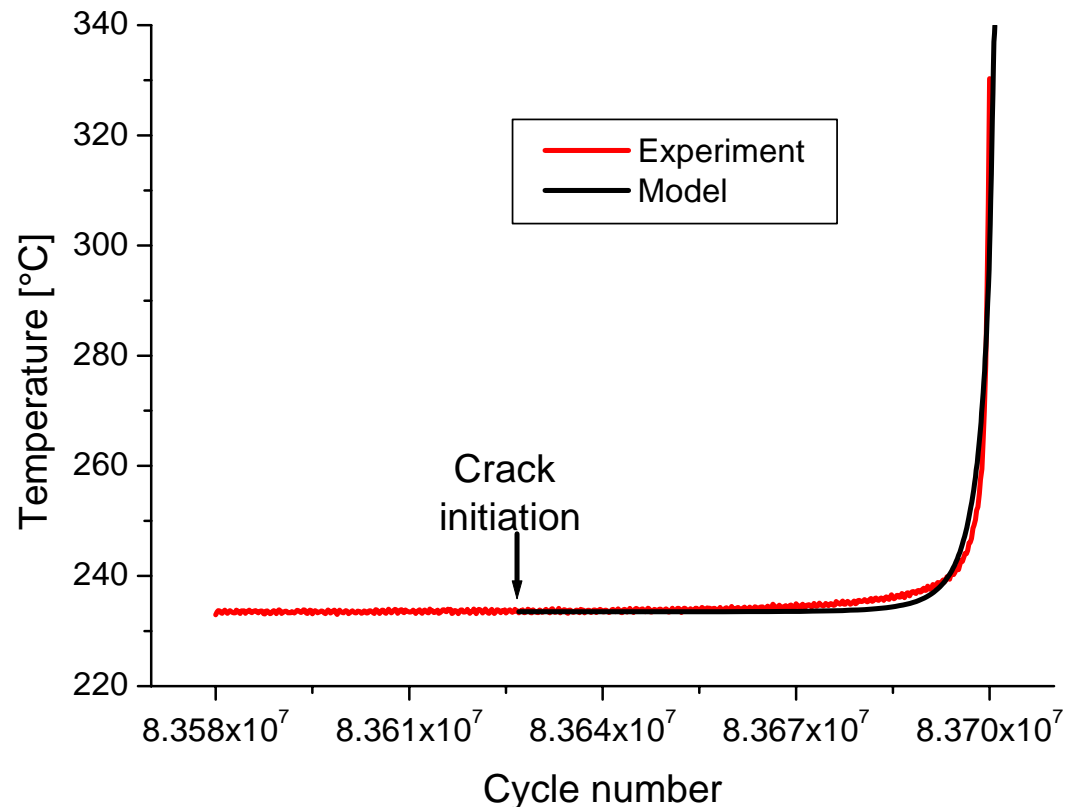
- The thermal problem is solve numerically with a finite element method:
 - Linear finite element
 - The integration scheme is implicit
 - The mesh is more refined in the zone close to the plan of crack propagation : 100 elements on the specimen radius
- Parameters of the simulation:
 - Initial crack radius: $a_0=8\mu\text{m}$
 - Eccentricity: $e=0.8$
 - Characteristic time: $t_c=4.4\text{s}$

Identification of the dissipated power P_0

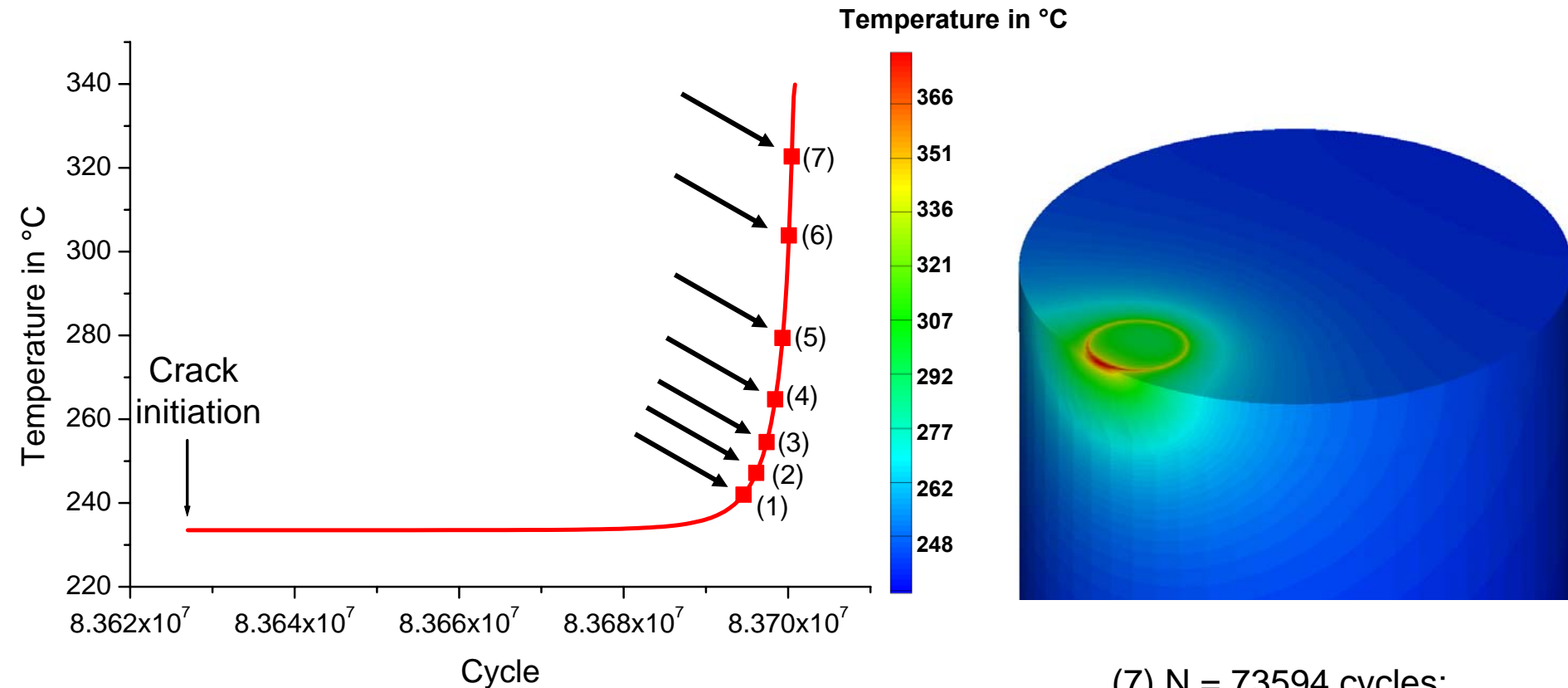
- Minimization of least squares method :

Minimization of least squares of the difference between the maximum temperature measured in experiments and the calculated temperature:

$$P_0 = 2.9 \text{ Wm}^{-1}$$



Numerical simulation associated to the experimental configuration

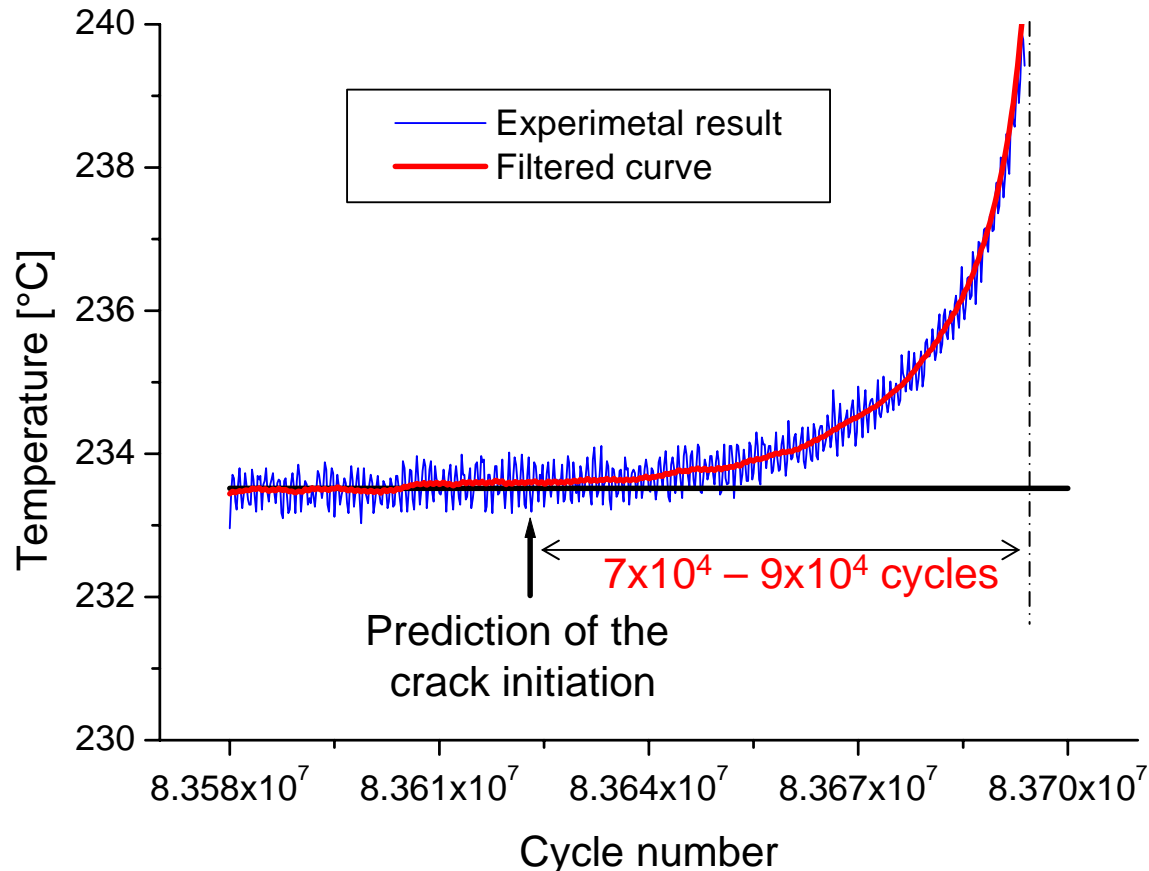


(7) $N = 73594$ cycles;
 $t = 3.68\text{s}$; $a = 0.270\text{mm}$

Experimental determination of the crack initiation

- **Experimental crack initiation criterion: increase of 0.07°C of the filtered temperature ($a \approx 0.02\text{mm}$)**
- **Crack propagation: between 7×10^4 and 9×10^4 cycles**

\Rightarrow very small part of the life of the specimen



Conclusion

- Experimental approach : temperature measurement during ultrasonic fatigue test
- Modeling of the thermal effect associated to the crack propagation :
 - Crack propagation
 - Dissipated power during crack growth
 - Modeling of the thermal problem and numerical solution
- Results
 - Good correlation with the experiment
 - Good estimation of the crack propagation duration